

- 2.13 a. We know that $P(S) = P(E_1 \cup E_2 \cup E_3 \cup E_4) = 1$ and, since the four events are pairwise mutually exclusive, $P(S) = P(E_1) + \dots + P(E_4) = .01 + ? + .09 + .81$. Thus $? = P(E_2) = 1 - .91 = .09$.
- b. $P(\text{at least one hit}) = P(E_1 \cup E_2 \cup E_3) = P(E_1) + P(E_2) + P(E_3) = .01 + .09 + .09 = .19$.

- 2.22 a. Let w_1 denote the first wine, w_2 the second, and w_3 the third. Then one sample point would be an ordered triple indicating the rank of each wine. For example, (w_1, w_2, w_3) would indicate that w_1 is superior to w_2 and w_3 while w_2 is superior to just w_3 .
- b. The sample space is given by all of the possible ordered triples. That is,
 $(w_1, w_2, w_3), (w_1, w_3, w_2), (w_2, w_1, w_3),$
 $(w_2, w_3, w_1), (w_3, w_1, w_2), (w_3, w_2, w_1)$
- c. Suppose w_1 is superior to w_2 and w_3 . Then the probability that the "expert" ranks w_1 as first or second is
 $P[(w_1, w_2, w_3) \text{ or } (w_1, w_3, w_2) \text{ or } (w_2, w_1, w_3) \text{ or } (w_3, w_1, w_2)] = 4/6 = 2/3$.

- 2.25 a. Define the events: E : family's income exceeds \$35,353
 N : family's income does not exceed \$35,353

Then the sample points are

$E_1: (EEEE)$	$E_2: (EEEN)$	$E_3: (EENE)$	$E_4: (ENEE)$
$E_5: (NEEE)$	$E_6: (EENN)$	$E_7: (ENEN)$	$E_8: (NEEN)$
$E_9: (ENNE)$	$E_{10}: (NENE)$	$E_{11}: (NNEE)$	$E_{12}: (ENNN)$
$E_{13}: (NENN)$	$E_{14}: (NNEN)$	$E_{15}: (NNNE)$	$E_{16}: (NNNN)$

- b. $A = \{E_1, E_2, \dots, E_{11}\}$
 $B = \{E_6, E_7, \dots, E_{11}\}$
 $C = \{E_2, E_3, E_4, E_5\}$
- c. By the definition of median $P(E) = P(N) = 0.5$. Therefore, each simple event is equally likely and $P(E_i) = \frac{1}{16}$. Then
 $P(A) = \frac{11}{16}$ $P(B) = \frac{5}{8}$ $P(C) = \frac{1}{4}$

2.30 $(4)(3)(4)(5) = 240$ by an application of the mn rule

2.35 $\binom{9}{3} \binom{6}{5} = \frac{9!}{3!5!1!} = 504$ ways

- 2.41 There are $\binom{50}{3} = 19,600$ ways to choose the three winners. Since the choice is random, each of the 19,600 sample points is equally likely.
- a. There are $\binom{4}{3} = 4$ ways for the organizers to win all of the prizes. Hence, the desired probability is $\frac{4}{19,600}$.
- b. The organizers can win exactly 2 of the prizes if 1 of the other 46 people wins 1 prize. Using the mn rule, there are $\binom{4}{2} \binom{46}{1} = 276$ ways for this to occur. Hence, the desired probability is $\frac{276}{19,600}$.
- c. $\binom{4}{1} \binom{46}{2} = 4140$. The probability is $\frac{4140}{19,600}$.
- d. $\binom{46}{3} = 15,180$. The desired probability is $\frac{15,180}{19,600}$.

- 2.44 The total number of ways to choose 4 students from 8 is $\binom{8}{4} = \frac{8!}{4!4!} = 70$. Since the choice is random, each of the 70 sample points is equally likely, and it remains only to determine how many sample points result in exactly 2 of the 3 undergraduates and 2 of the 5 graduates. Using the mn rule, this number is $\binom{3}{2} \binom{5}{2} = 3(10) = 30$ and the desired probability is $\frac{30}{70} = \frac{3}{7}$.

- 2.48 Refer to Theorem 2.3. The total number of ways to divide the 9 motors into 3 groups of size 3 is $\frac{9!}{3!3!3!}$. If both of the motors from a particular supplier are assigned to the first line, there are only 7 motors to be assigned, one to line 1 and 3 each to lines 2 and 3. This can be done in $\frac{7!}{1!3!3!}$ ways. Hence the probability of interest is

$$\frac{\binom{7}{1} \binom{6}{3} \binom{3}{3}}{\binom{9}{3} \binom{6}{3} \binom{3}{3}} = \frac{7!3!}{9!} = \frac{1}{12}$$

2.50 $6! \left(\frac{1}{6}\right)^6 = \frac{5}{324}$